

Elasticity Analysis of Web Browsing Behavior of Users

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-----ABSTRACT-----

There are many browsers available in the market but only a few are liked and used by many. Every browser has a predefined level of popularity in the market. This paper considers the setup of only two browsers installed in a computer system and a user prefers to any one of them and if fails, switches to the other one. Elasticities of browser sharing are derived, index formation and graphical study are performed to compare the simulated output.

Keywords: Markov Chains (MC), Transition Probability Matrix (TPM), Quality of Service (QOS), Browser Failure (BF).

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I. INTRODUCTION

For internet surfing many browsers are available in the market which can be used to connect a particular website as required by users. Every browser bears a failures rate related to connectivity. It occurs because of internal coding structure of browser, command execution pattern and speed of search engine. It is termed as browser failure (BF) and has some probability of occurrence every moment. Every browser serves to user and, therefore, has certain quality of service (QOS) also. Shukla and Singhai (2010) examined the web browsing behavior of user by a Markov chain model. This paper extends the same approach under elasticity property based approach and analysis.

The elasticity is a property defined as rate of change of one parameter with respect to another subject to condition when all other parameters are constant. This kind of study helps in decision making regarding continuity or stopping the process. Iso-curves are those showing the output when a level of input is fixed. In other words iso-curves are possible adjustments between two parameters. Index formation is a technique that shows the impact of relative change. This paper incorporates Elasticities analysis, iso-curve analysis and index formation on the contribution of Shukla and Singhai (2011).

II. A REVIEW

Catledge and Pitkow (1995) presented a contribution on characterization of browsing strategies. Pirolli. and pitkow (1996) suggested usable structure for web in light of many users. A similar study is performed due to pitkow (1997) regarding search of reliable usage data on www. Naldi (2002) presented Markov chain model based study in a multioperator environment. The detailed distribution of basics of Markov Chain Model is in Medhi (1991) and web browsing details are in Han and Kamber (2001). Shukla et al. (2007) discussed stochastic model for space decision switches for complete network. Shukla et al. (2007 a, b, c) suggested the use of Markov chain model in networking and operating system analysis. Shukla and Jain (2007) used Markov chain model for the analysis of multilevel Queue Scheduler in operating system. Shukla and Singhai (2010 a) discussed traffic analysis of message flow in three crossbar architecture space division switches. Deshpande & Karypis (2004) discussed selective Markov chain model for predicting webpage access. Shukla et al. (2010 a, b, c, d, e, f, g, h,) discussed different aspects on Markov chain model in determining the system behavior. Shrivastava et al. (2000) presented a thought oriented contribution on the web page mining and application of

usage patterns from web data. Shukla et al. (2011) is also a useful contribution.

Objective of this content are:

1. To examine Elasticities of browser blocking,
2. To study iso-curve of parameters,
3. To develop index for performance indications.

Let $\{X_n, n \geq 0\}$ be a Markov chain on state space $\{C, Q, B_1, B_2, S\}$ see Shukla and Singhai (2011) where

State C: represents connecting state.

State Q: user quitting from the proce

State B₁: user attempts to surf through browser B₁.

State B₂: user attempts to surf through browser B₂.

State S: success for connectivity and surfing.

The $X^{(n)}$ denotes the position of random variable X in the state space at the nth browser connectivity attempt made by a web user.

III. ASSUMPTIONS FOR USER BROWSING BEHAVIOR [see Shukla and Singhai (2011)]

- (1) The user attempts for dial up connection to use Internet. If the connection is not established, user quits with the probability P_c .
- (2) When connection is made user chooses any one of browsers B_1, B_2 with the probability p and $1-p$ respectively.
- (3) User navigates to any one browser at a time when successfully opened.
- (4) Browser B_i ($i=1, 2$) failure occurs due to non-opening of any site through browser B_i . Then user either quits (with probability p_q) or switches to the next browser.
- (5) Switching between browsers are on attempt by attempt basis ($n=1, 2, 3, \dots$).
- (6) Initial preference for a browser is based on quality of services and variety of facility features are contained in both browsers.
- (7) Failure probability of a browser B_1 is b_1 and of B_2 is b_2 .
- (8) Transition probability of surfing through B_1 , being completed in a single attempt is $(1 - b_1)$.
- (9) Absorbing state (transition from a state to itself) probability is 1. No further transition from this state occurs.

Under these assumptions user's browsing behavior is discussed in this paper by a Markov Chain Model (see fig.3.1) in which the transition probabilities are on the arcs connecting the circles and representing the chain states.

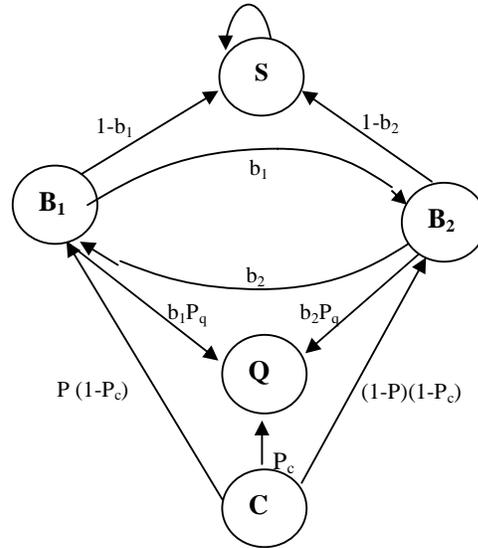


Fig. 3.1 [Transition Diagram of user browsing]

The initial conditions $n=0$, (state probability before the first surf attempt) are:

$$\left. \begin{aligned} P[X^{(0)} = C] &= 1 \\ P[X^{(0)} = B_1] &= 0 \\ P[X^{(0)} = B_2] &= 0 \\ P[X^{(0)} = S] &= 0 \\ P[X^{(0)} = Q] &= 0 \end{aligned} \right\} \dots (3.1)$$

The unit-step transition probability matrix is:

	B ₁	B ₂	S	Q	C
B ₁	0	$b_1(1-b_1)$	$(1-b_1)$	b_1P_q	0
B ₂	$b_2(1-b_2)$	0	$(1-b_2)$	b_2P_q	0
S	0	0	1	0	0
Q	0	0	0	1	0
C	$P(1-P_c)$	$(1-P)(1-P_c)$	0	P_c	0

Table: 3.1 [Transition Probability Matrix]

Using Shukla and Singhai (2011) we can write.

$$\begin{aligned} P[X^{(2n)} = B_1] \\ = b_1^{n-1} b_2^n (1-P)(1-P_c)(1-P_q)^{2n-1}; n > 0 \dots (3.2) \end{aligned}$$

$$P[X^{(2n+1)} = B_1] = (b_1 b_2)^n P(1 - P_C)(1 - P_q)^{2n}; n > 0 \dots (3.3)$$

Similarly, for browser B₂

$$P[X^{(2n)} = B_2] = b_1^n b_2^{n-1} P(1 - P_C)(1 - P_q)^{(2n-1)}; n > 0 \dots (3.4)$$

When n is odd

$$P[X^{(2n+1)} = B_2] = (b_1 b_2)^n (1 - P)(1 - P_C)(1 - P_q)^{2n}; n > 0 \dots (3.5)$$

IV. BROWSER SHARING

The probability that navigation successfully starts with browsers B₁ at the nth attempt [as discussed by Shukla and Singhai (2010)]

$$P_1^{(n)} = P[X^{(n-1)} = B_1] \cdot P[X^{(n)} = S | X^{(n-1)} = B_1] \quad n > 0 \dots (4.1)$$

$$P_1^{(n)} = (1 - b_1) \sum_{i=1}^n P[X^{(i-1)} = B_1] \quad \dots (4.2)$$

Let $b_1 b_2 (1 - P_q)^2 = r$

For n > 0; when n is even [Using Shukla and Singhai (2011)]

$$P^{(2n)} = (1 - b_1) \left[P(1 - P_C) \left\{ \frac{1 - r^n}{1 - r} \right\} + (1 - P)(1 - P_C)(1 - P_q) b_2 \left\{ \frac{1 - r^{n-1}}{1 - r} \right\} \right] \dots (4.3)$$

For n > 0; when n is odd

$$P^{(2n+1)} = (1 - b_1) \left\{ \frac{1 - r^n}{1 - r} \right\} \left[P(1 - P_C) + (1 - P)(1 - P_C)(1 - P_q) b_2 \right] \quad \dots (4.4)$$

These two equations exhibit the overall probability of sharing two browsers by a user in a web environment. These two proportions also reflect how the sharing of two

different browsers change with respect to the initial preference. The limiting cumulative probabilities of successful surfing through the two browsers can be obtained by taking the limit of expression over infinite attempts i.e. when the numbers of attempts are infinitely large.

When n is even

$$P_1 = \lim_{n \rightarrow \infty} \overline{P_1}^{(2n)} = (1 - b_1)(1 - P_C) \left[\frac{P + (1 - P)(1 - P_q) b_2}{1 - b_1 b_2 (1 - P_q)^2} \right] \dots (4.5)$$

When n is odd

$$P_1 = \lim_{n \rightarrow \infty} \overline{P_1}^{(2n+1)} = (1 - b_1)(1 - P_C) \left[\frac{P + (1 - P)(1 - P_q) b_2}{1 - b_1 b_2 (1 - P_q)^2} \right] \dots (4.6)$$

These expressions are independent of parameter n. Browser sharing depends on p, p_q, b₁, b₂ and p_c.

V. ELASTICITIES OF BROWSER SHARING

Differentiate p₁ with respect to b₁

$$f_1(\cdot) = \left(\frac{\partial p_1}{\partial b_1} \right)_{b_2, p_c, p_q, p} = \frac{(1 - p_c) \{ p + (1 - p)(1 - p_q) b_2 \} [\{ (1 - b_1) b_2 (1 - p_q)^2 \} - \{ 1 - b_1 b_2 (1 - p_q)^2 \}]}{[1 - b_1 b_2 (1 - p_q)^2]^2} \dots (5.1)$$

Differentiate p₁ with respect to b₂

$$f_2(\cdot) = \left(\frac{\partial p_1}{\partial b_2} \right)_{b_1, p_c, p_q, p} = \frac{(1 - b_1)(1 - p_c) [1 - p_q \{ b_1 (1 - p_q) \{ p + (1 - p) \} + (1 - p) \}]}{[1 - b_1 b_2 (1 - p_q)^2]^2} \dots (5.2)$$

Differentiate p₁ with respect to p_c

$$f_3(\cdot) = \left(\frac{\partial p_1}{\partial P_C} \right)_{b_1, b_2, p_q, p} = (1 - b_1) \left[\frac{p + (1 - p)(1 - p_q) b_2}{b_1 b_2 (1 - p_q)^2 - 1} \right] \dots (5.3)$$

VI. ISO-QUIETING CURVE

$$p_c = \frac{\{p + (1-p)(1-pq)b_2\}}{(1-b_1) - p_1 \{1 - b_1 b_2 (1-pq)^2\}} \dots\dots\dots (6.1)$$

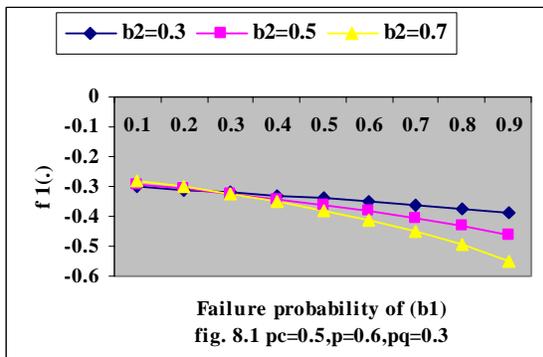
VII. Browser Popularity Index (BPI)

We define BPI as

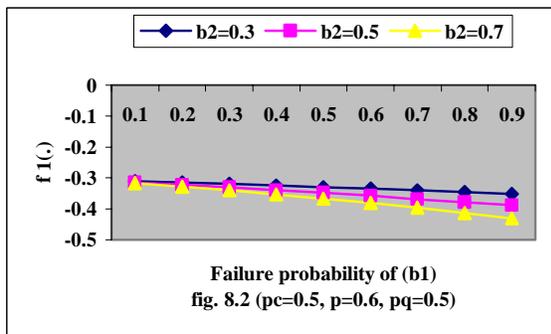
$$I(B_1) = \frac{P_1}{P_1 + P_2}$$

$$I(B_1) = \frac{[(1-b_1)(1-p_c)[p+(1-p)(1-pq)b_2]}{[(1-b_1)(1-p_c)\{p+(1-p)(1-pq)b_2\} + (1-b_2)(1-p_c)(1-p) + p(1-pq)b_1]} \dots\dots\dots (7.1)$$

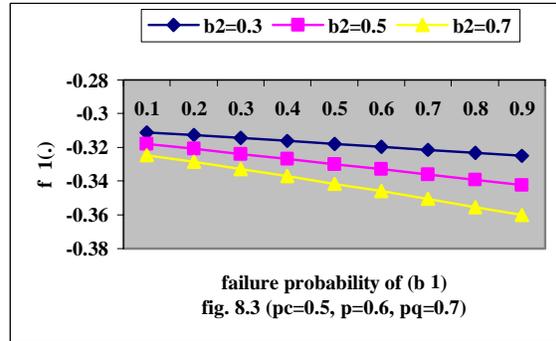
VIII. SIMULATION STUDY



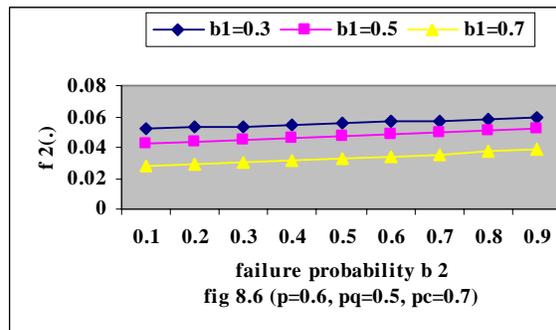
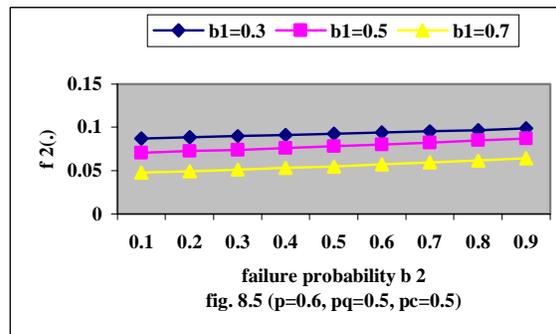
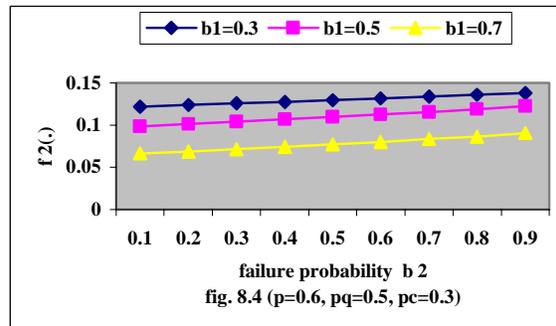
In view of figure 8.1 if browser blocking is high the elasticities of browser share decrease with constant rate slowing adverse effect on browser sharing. If b₂ is high then this effect is more serious, specially at while p_q = 0.3



In figure 8.2, when p_q is 0.5 (higher a earlier), the elasticities are more negative than earlier, but having similar pattern.



In figure 8.3 contains high value of p_q = 0.7 and due to this the stability in elasticity appears better. It seems if p_q is high the elasticity factor f₁ (.) shall be stable.



When to examine elasticities with respect to b₂ as obtain in f₂ (.), the output in figure 8.4-8.6 are showing reverse

pattern. With the increase of b_2 , $f_2(\cdot)$ has increasing pattern. On the p_c probability if high contains a stability factors in Elasticities variation. The elasticity reduces with the combined increment in b_1 and p_c both.

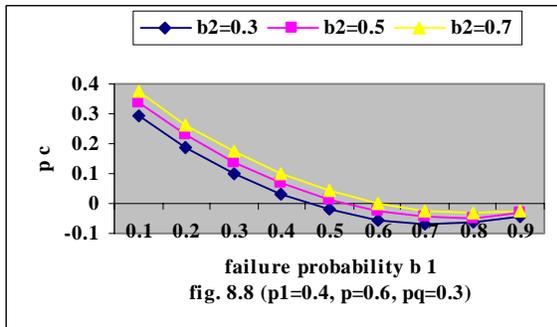
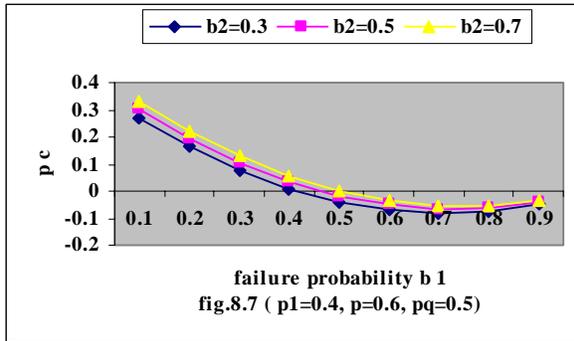


Figure 8.7, 8.8 show downward trend for increasing value of b_1 . When b_2 is high better gain appears to probability p_c . The iso-quieting curves to b_1 are of exponential nature.

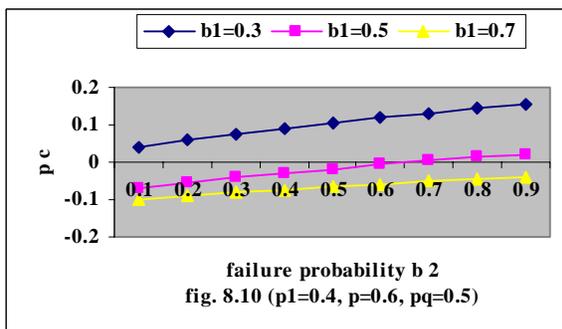
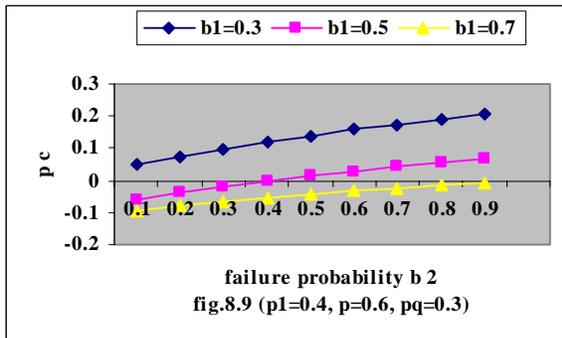


Figure 8.9, 8.10 are showing the linear trend when b_2 is increasing constantly. The trend line goes down while b_1 is high. These iso-quieting curves are positive in nature as discussed earlier.

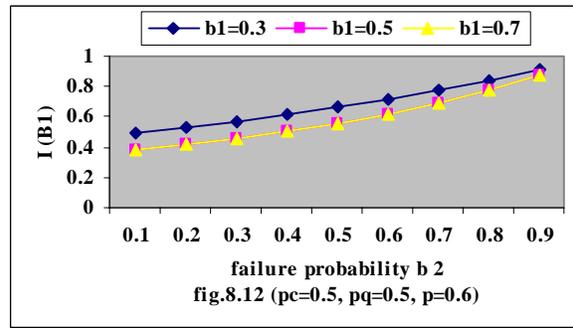
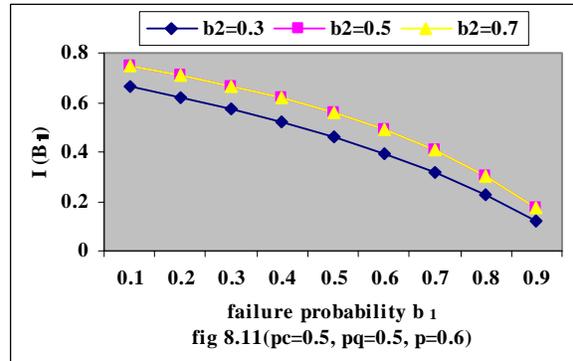


Figure 8.11, 8.12 relate to browser share index. This index depends on b_1, b_2 probabilities. The increment in b_1 reduces the index level where as increase in b_2 increases the index level where as increase in b_2 increases the same. This index shows the relative browser sharing chance in light of browser blocking probability.

XI. CONCLUDING REMARKS:

The elasticity pattern found negative with respect to b_1 for first browser but opposite in nature for second browser. This indicates that a browser has to keep lesser blocking level comparing to other in order to maintain the same popularly level. The quieting probability is a function of browser blocking probability therefore a fair balance must be maintained between these two. The relative increment in browsing index shows that input parameters must be present in a particular interval to maximize the index values.

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